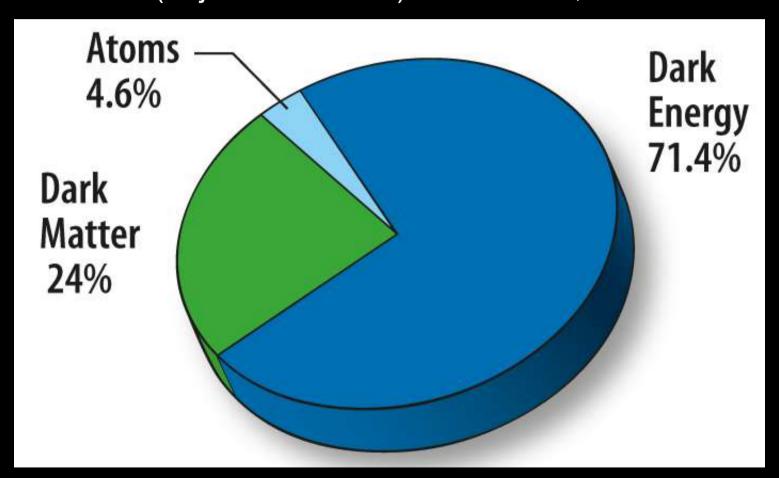
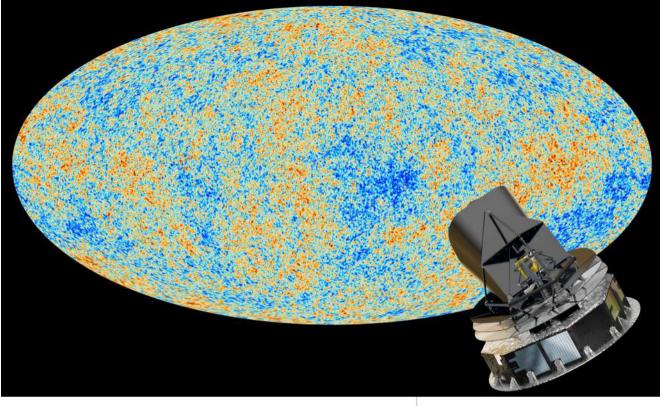
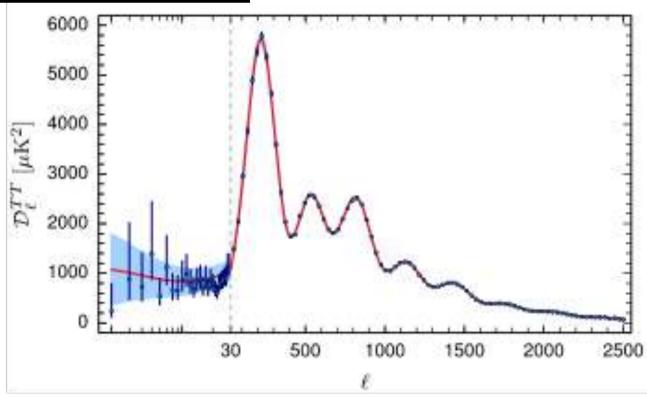
The "Missing baryons"—what is it? Where is it? How much?

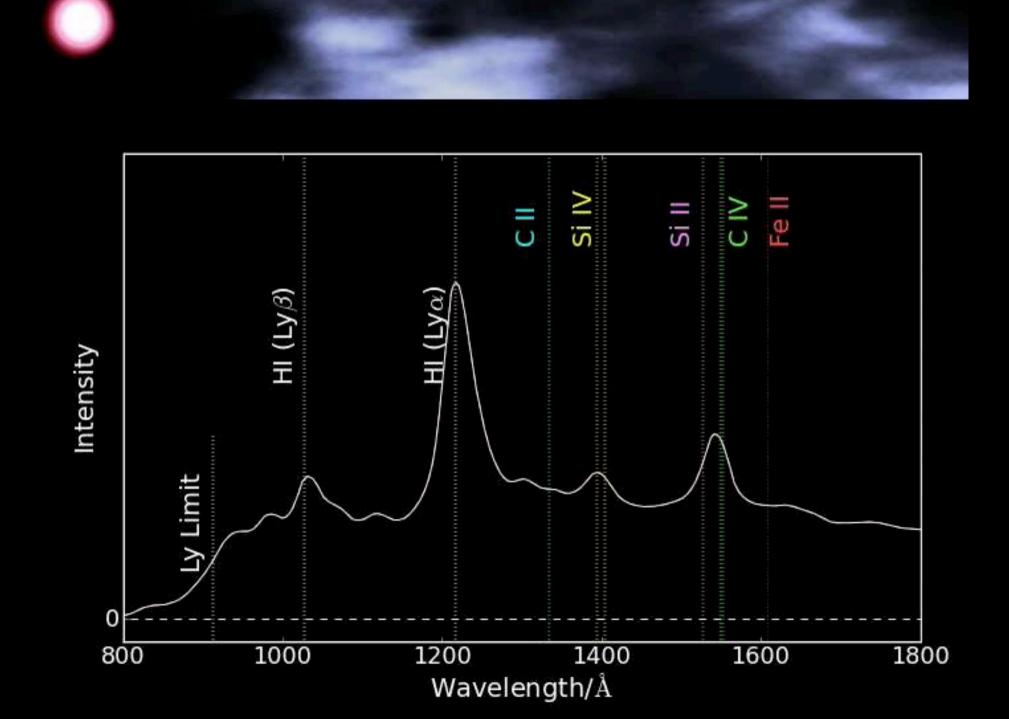
Yin-Zhe Ma (马寅哲)
University of KwaZulu-Natal, South Africa (Adjunct Professor) NAOC/PMO, CAS

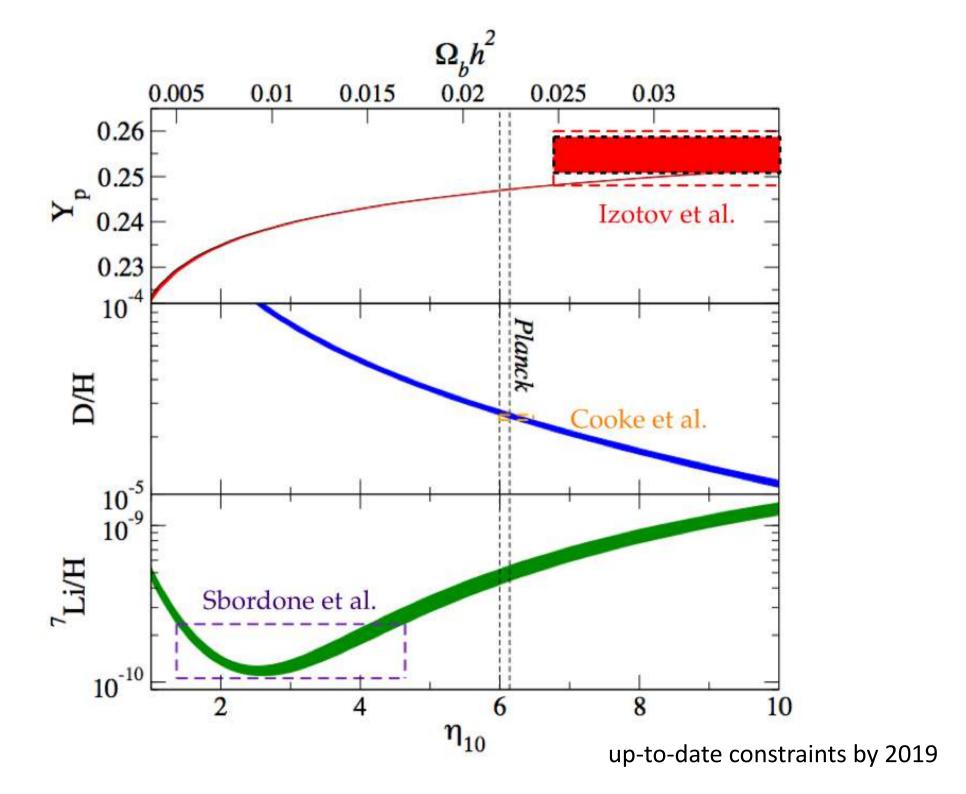


Collaborators: R. Battye, D. Contreras, C. Dickinson, C. Hernandez-Monteagudo, G. Hinshaw, A. Hojjati, Y.-C. Li, I. McCarthy, K. Moodley, M. Remazeilles, D. Scott, L. Staveley-Smith, H. Tanimura, D. Tramonte, L. Van Waerbeke, J. Zuntz, & Planck team



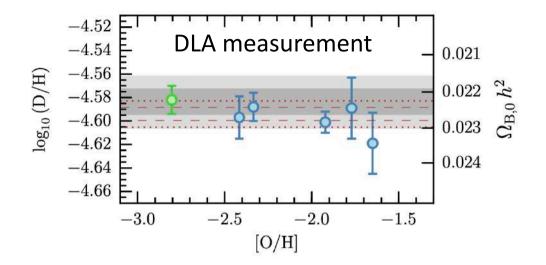






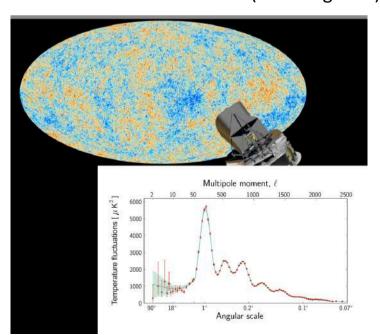
 $\boxed{100\Omega_{\rm b}h^2({\rm BBN}) = 2.260 \pm 0.018 \pm 0.029}$

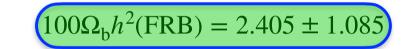
Cooke+ 2016



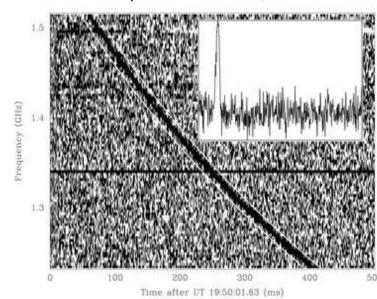
 $100\Omega_{\rm b}h^2({\rm CMB}) = 2.226 \pm 0.023$

Planck collaboration 2018 (including YZM)

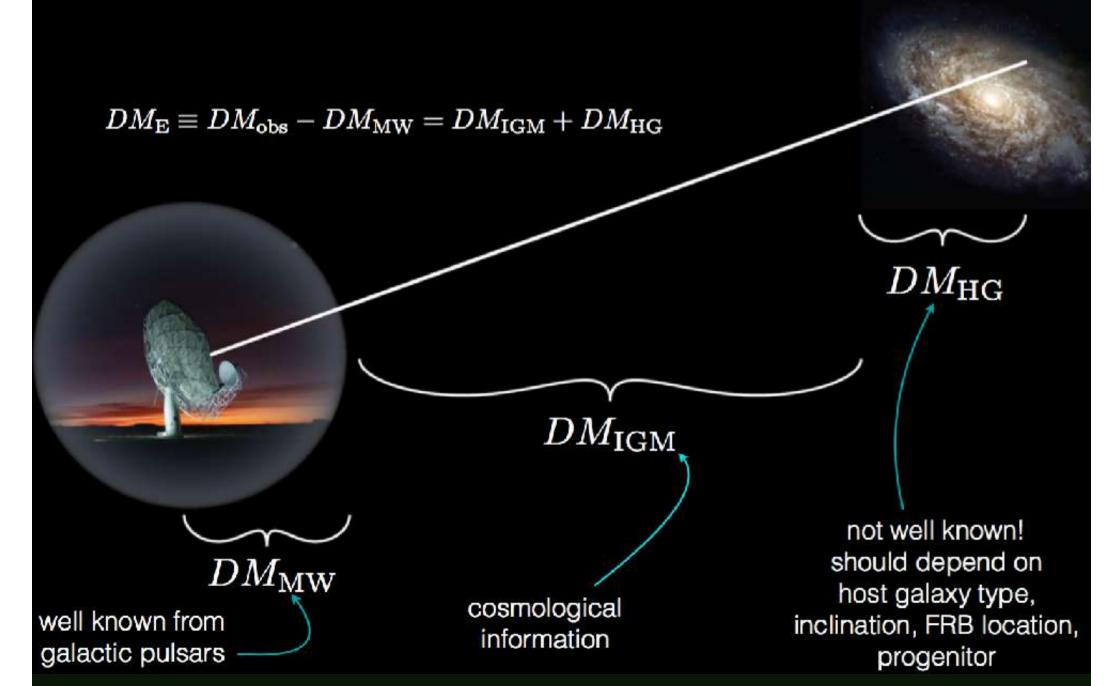


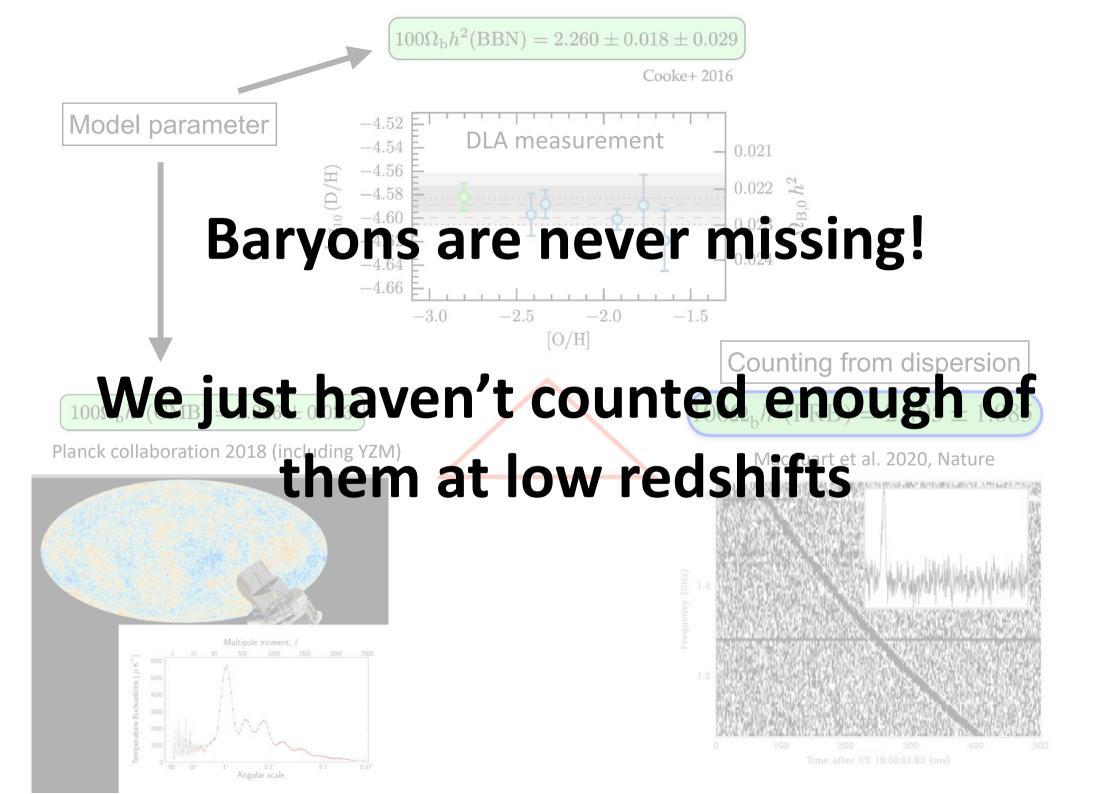


Macquart et al. 2020, Nature



Contributions to DM





Cosmic baryon inventory:

Category	Parameter	Components ^a
3.3	Main-sequence stars: spheroids and bulges	0.0015 ± 0.0004
3.4	Main-sequence stars: disks and irregulars	0.00055 ± 0.00014
3.5	White dwarfs	0.00036 ± 0.00008
3.6	Neutron stars	0.00005 ± 0.00002
3.7	Black holes	0.00007 ± 0.00002
3.8	Substellar objects	0.00014 ± 0.00007
3.9	H I + He I	0.00062 ± 0.00010
3.10	Molecular gas	0.00016 ± 0.00006
3.11	Planets	10^{-6}
3.12	Condensed matter	$10^{-5.6 \pm 0.3}$
3.13	Sequestered in massive black holes	$10^{-5.4}(1+\epsilon_n)$

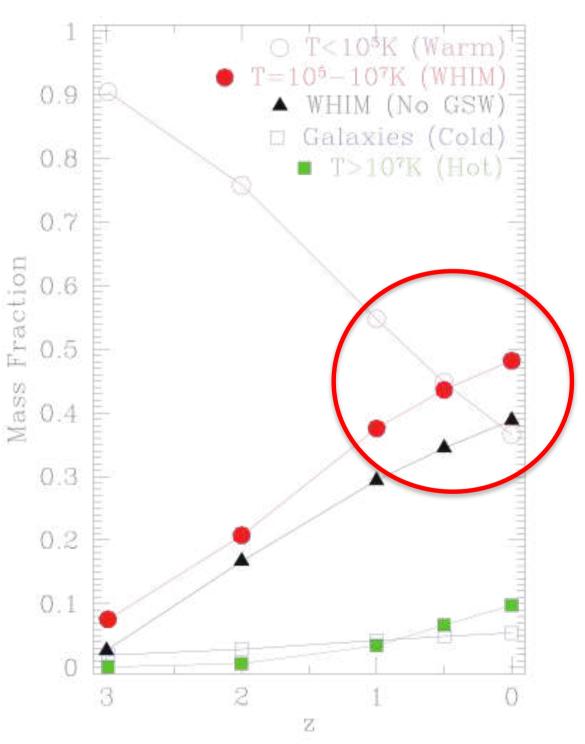
3.3+...+3.13:
$$\Omega_{b,g} = 0.0035$$
 =8% total baryon density

90% of baryons are in either intergalactic or intercluster medium



Cen and Ostriker 2006

X-ray: ~ $n_{\rm e}^2(r)$





Weak Lensing

YZM, L. Van Waerbeke et al., 2015, JCAP, 09, 046
A. Hojjati, I. McCarthy, J. Harnois-Deraps, **YZM** et al., 2015, JCAP, 10, 047
A. Hojjati,, **YZM**,... 2017, JCAP, 471, 1565

Thermal SZ maps



Luminous red galaxies

H Tanimura, ..., YZM,... et al. 2018, MNRAS, 483, 223

kinetic Sunyaev-Zeldovich effect



Peculiar velocity field

Planck intermediate results XXXVII, 2016, A&A, 586, 140 C.Hernandez-Monteagudo, **YZM**, F-S Kitaura, W.Wang et al., 2015, Phys. Rev. Lett. 115, 191301 Yi-Chao Li, **YZM**, Mathieu Remazeilles, Kavilan Moodley, 2018, PRD, 97, 023514

kinetic SZ effect



MCXC clusters

The Observation of Relic Radiation as a Test of the Nature of X-Ray Radiation from the Clusters of Galaxies

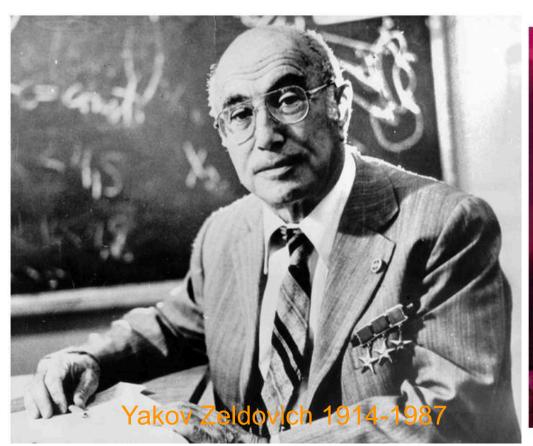
1972

The velocity of clusters of galaxies relative to the microwave background. The possibility of its measurement

R. A. Sunyaev and Ya. B. Zeldovich Academy of Sciences, USSR, Space Research Institute, Profsoyuznaja 88, 117810 Moscow, USSR

Received 1979 May 31

1980







Weak Lensing

YZM, L. Van Waerbeke et al., 2015, JCAP, 09, 046 A. Hoiiati, I. McCarthy, J. Harnois-Deraps, YZM et al., 2015, JCAP, 10, 047 A. Hojjati, , YZM,... 2017, JCAP, 471, 1565



Thermal SZ maps X Luminous red galaxies

H Tanimura, ..., **YZM**,... et al. 2018, MNRAS, 483, 223

—>HI (21-cm) intensity mapping X Central galaxies

D. Tramonte, YZM, Y.C. Li, L. Staveley-Smith, 2019, MNRAS

kinetic Sunyaev-Zeldovich effect



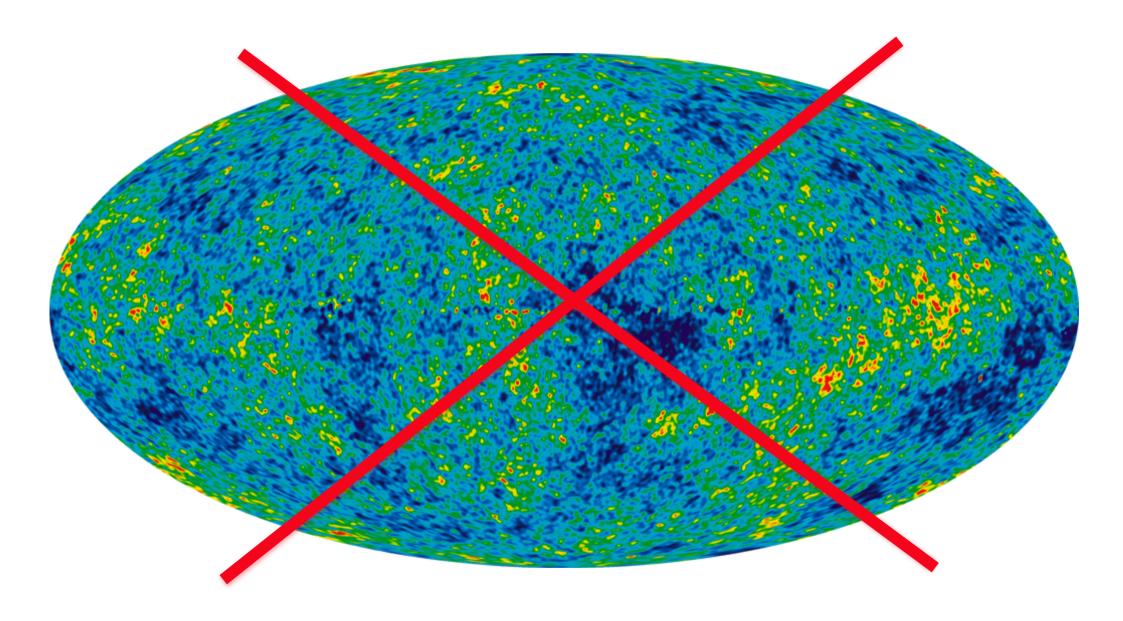
Peculiar velocity field

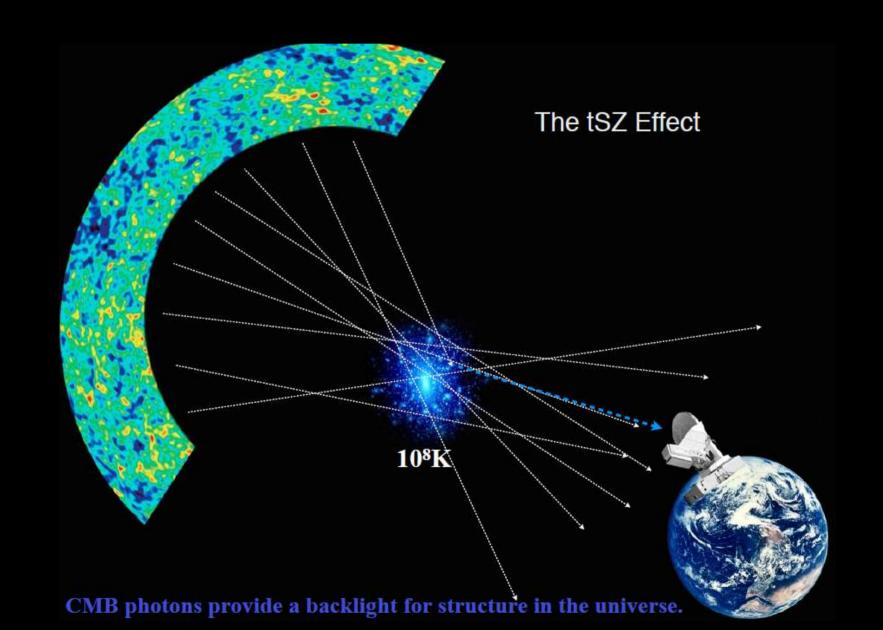
Planck intermediate results XXXVII, 2016, A&A, 586, 140 C.Hernandez-Monteagudo, YZM, F-S Kitaura, W.Wang et al., 2015, Phys. Rev. Lett. 115, 191301 Yi-Chao Li, YZM, Mathieu Remazeilles, Kavilan Moodley, 2018, PRD, 97, 023514

kinetic SZ effect

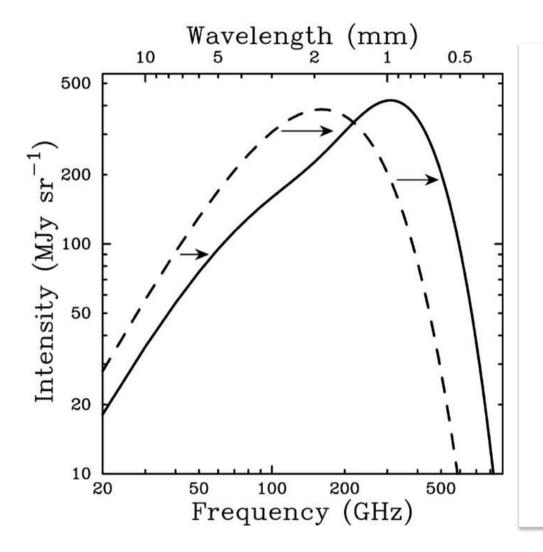


X MCXC clusters





Thermal Sunyaev-Zeldovich effect (tSZ):

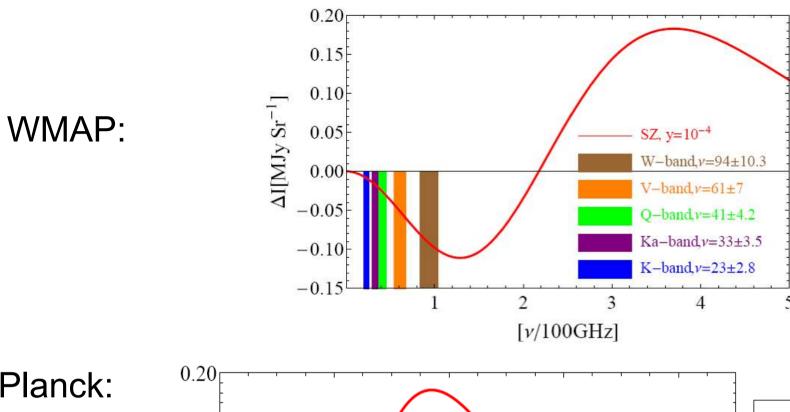


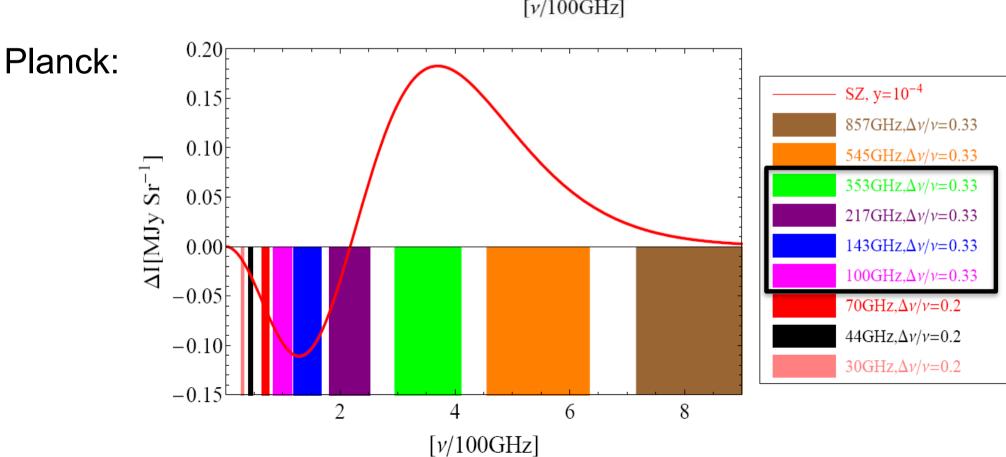
$$\frac{\Delta T}{T} = \left[\eta \frac{e^{\eta} + 1}{e^{\eta} - 1} - 4 \right] y \equiv g_{\nu} y$$

$$g_{\nu} \equiv (\eta (e^{\eta} + 1) / (e^{\eta} - 1)) - 4$$

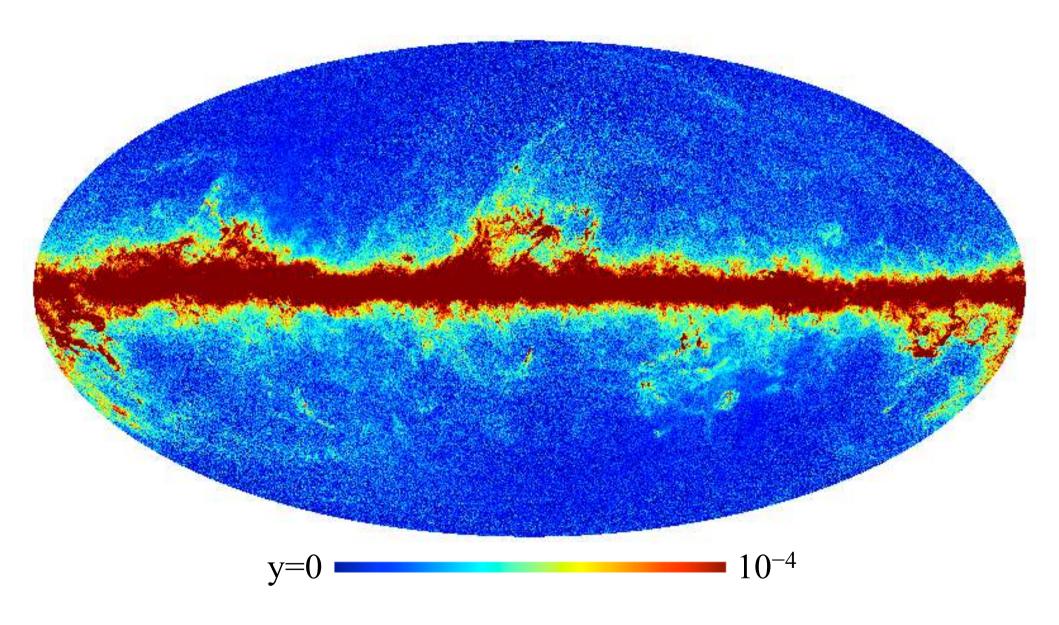
$$\eta = \frac{h\nu}{k_B T_{\text{CMB}}} = \frac{h\nu_0}{k_B T_0} = 1.76 \left(\frac{\nu_0}{100 \text{GHz}} \right)$$

$$y = \frac{k_B \sigma_T}{m_e c^2} \int_0^l T_e(l) n_e(l) \, dl$$





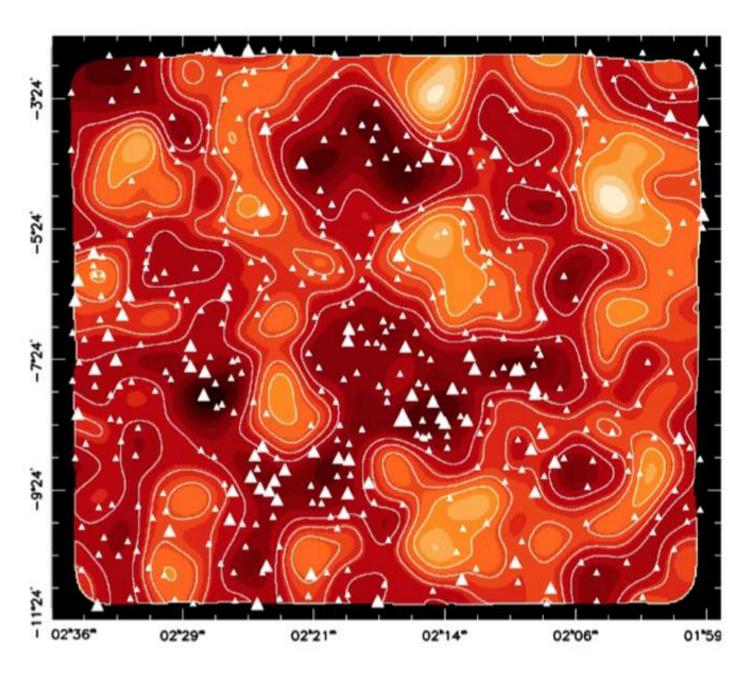
Planck SZ y map, version E



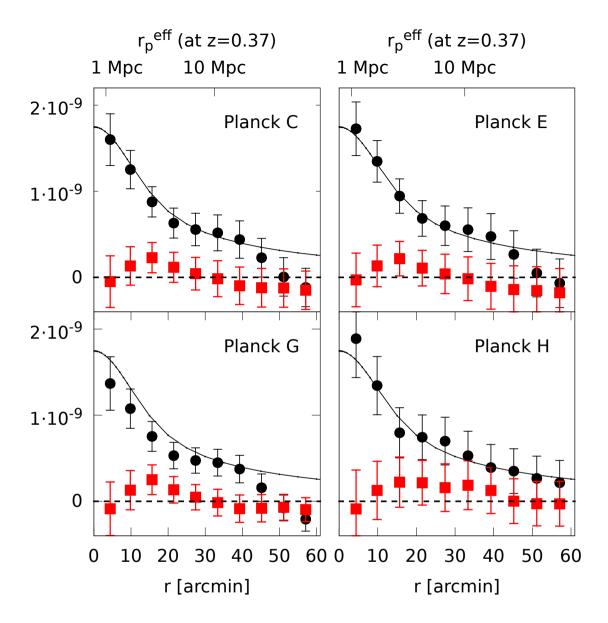
Reject $\beta_{dust} = 2.0$, $r_{2.0}(100 \text{ GHz}) = 0$

CFHT mass map:

154 deg^2 in 4 patches

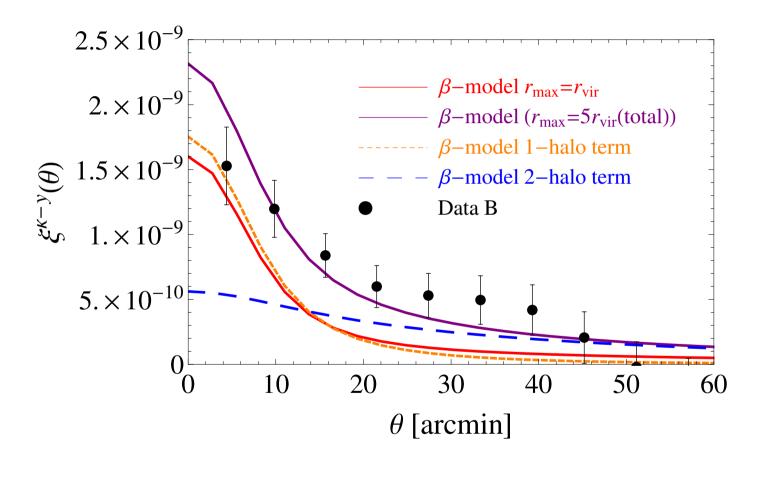


Van Waerbeke et al., 2014, MNRAS



Red squares are for cross-correlation with lensing B-mode

Halo model:



Ma et al. fits a halo model to the observed correlation function. A β model fits well, but in this context the data requires a 2-halo term to fit the large angular scale separation.

Virial theorem with
$$z=0.37$$
, $M=10^{12}-10^{16} {\rm M}_{\odot}$
$$\qquad \qquad \downarrow$$

$$T_{\rm e}=10^5-10^7 {\rm \, K}$$

Red Cluster Sequence Lensing Survey (RCSLenS) X Planck thermal SZ effect map

Sky coverage: 560 deg² 8.4 sigma detection

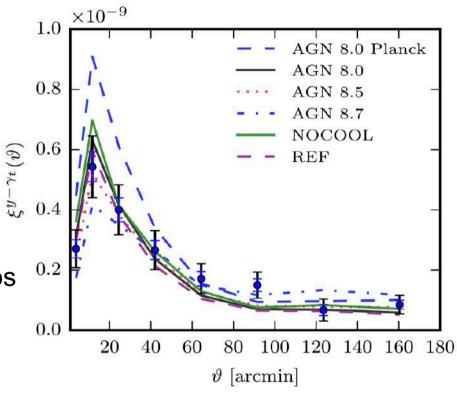
A. Hojjati,, YZM,... 2017, JCAP, 471, 1565

Recent works:

(1) DES Y3 lensing data X Planck+ACT maps -21σ C.L.

Gatti, et al., arXiv: 2108.01600

Pandey, et al., arXiv: 2108.01601



(2) KiDS X Planck+ACT SZ maps -9σ C.L Troster et al., arXiv: 2109.04458



Weak Lensing

YZM. L. Van Waerbeke et al., 2015, JCAP, 09, 046 A. Hojjati, I. McCarthy, J. Harnois-Deraps, YZM et al., 2015, JCAP, 10, 047 A. Hojjati, , YZM,... 2017, JCAP, 471, 1565

Thermal SZ maps



Luminous red galaxies

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kinetic Sunyaev-Zeldovich effect



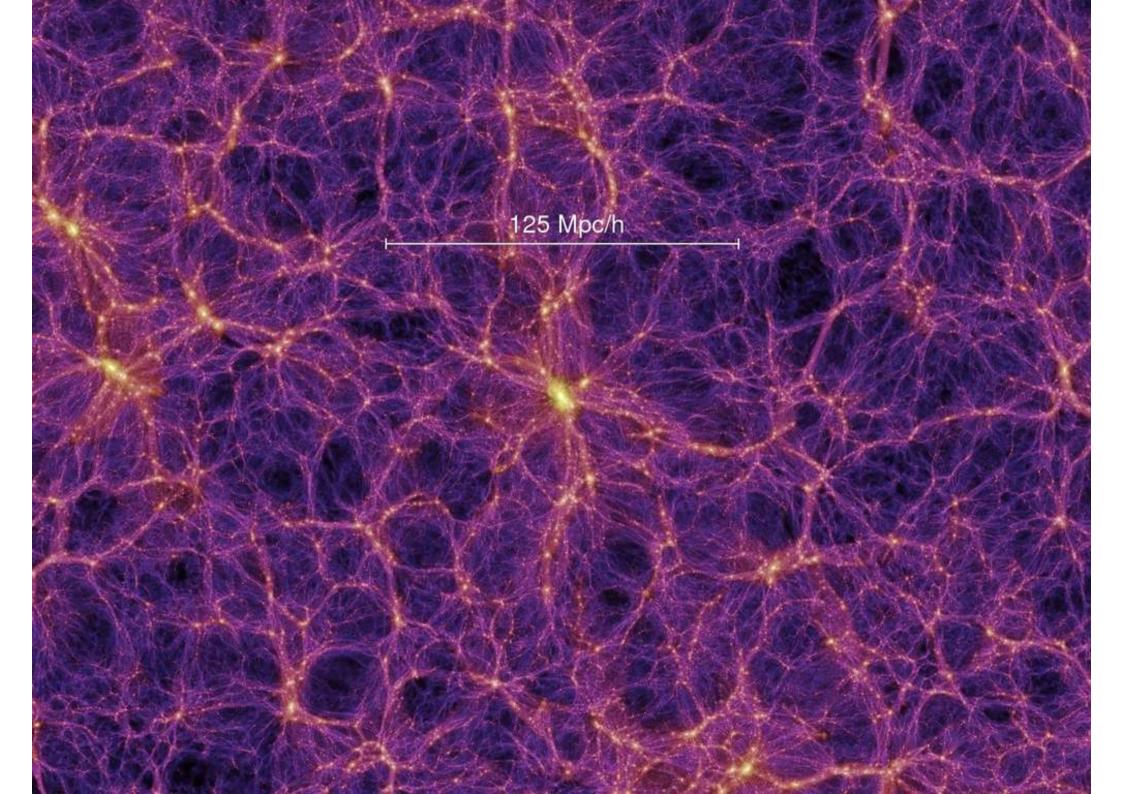
Peculiar velocity field

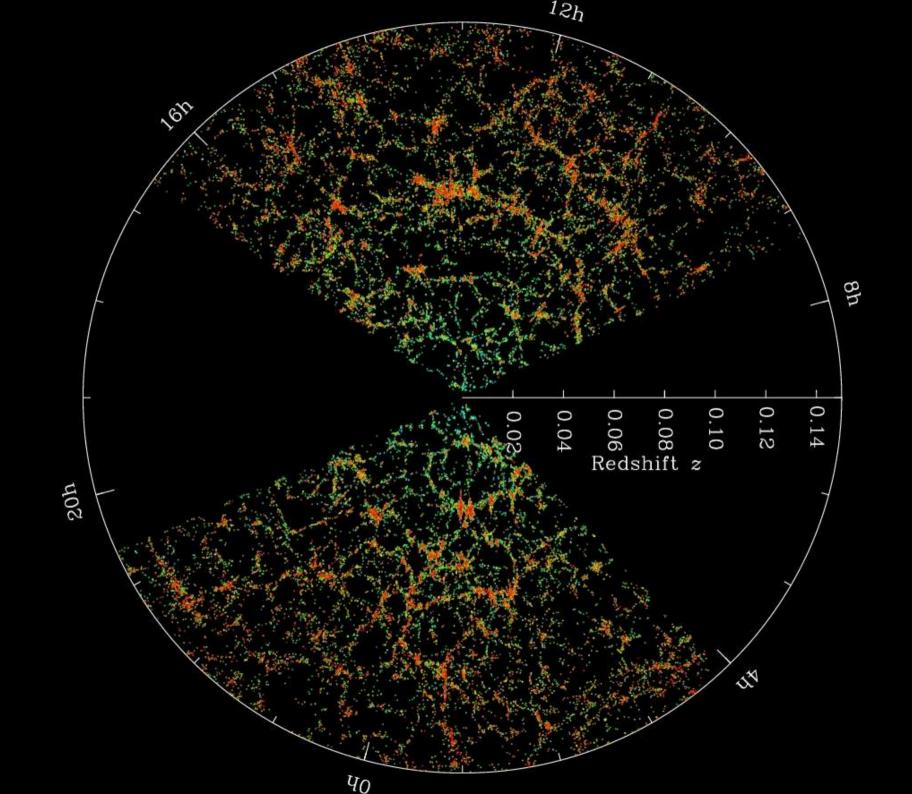
Planck intermediate results XXXVII, 2016, A&A, 586, 140 C.Hernandez-Monteagudo, YZM, F-S Kitaura, W.Wang et al., 2015, Phys. Rev. Lett. 115, 191301 Yi-Chao Li, YZM, Mathieu Remazeilles, Kavilan Moodley, 2018, PRD, 97, 023514

kinetic SZ effect



X MCXC clusters

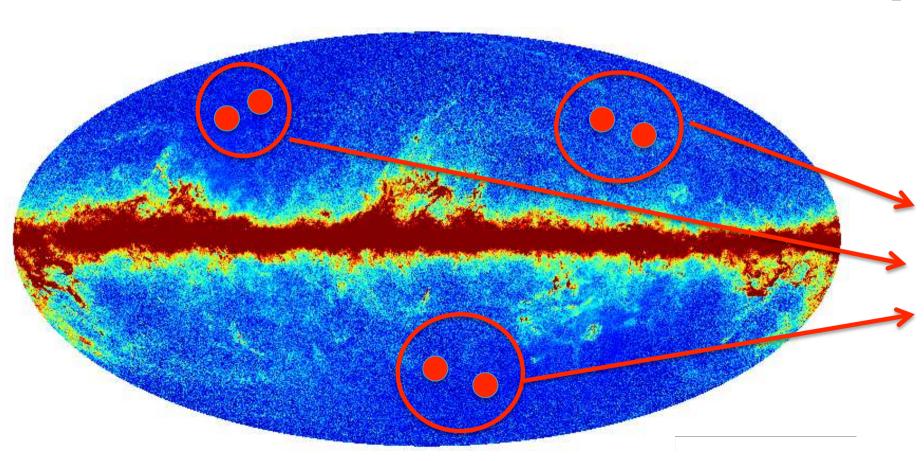


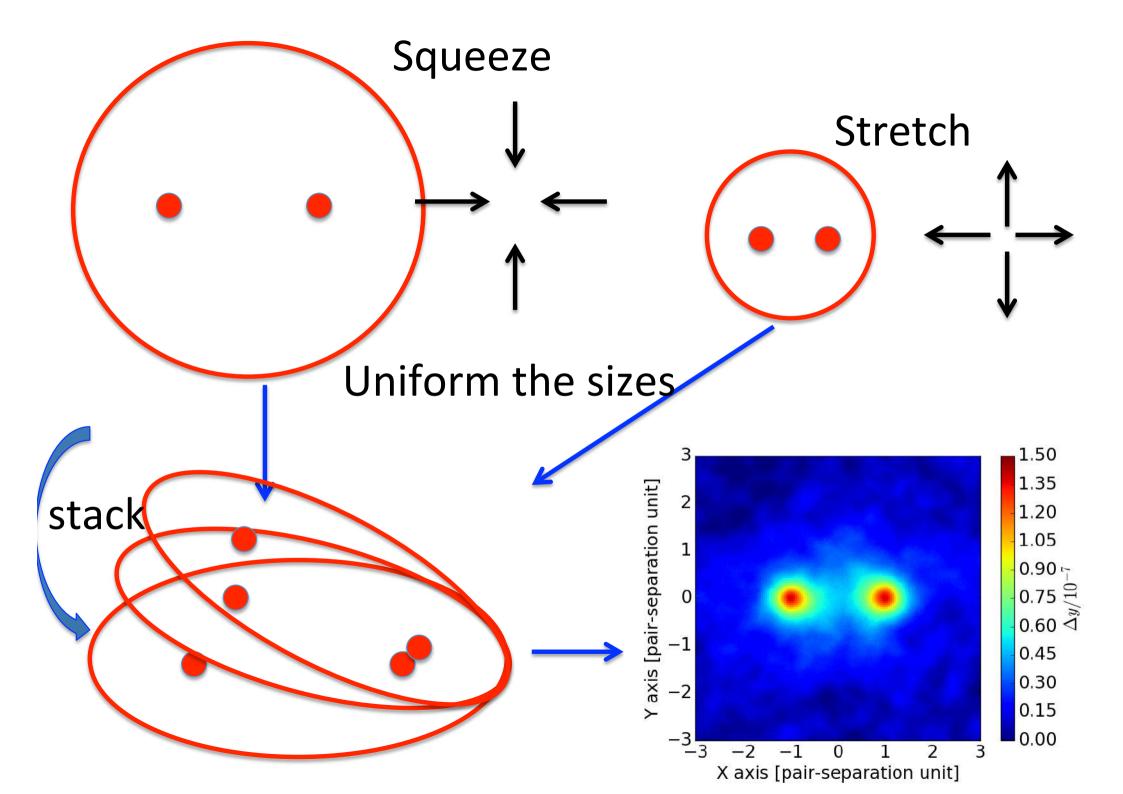


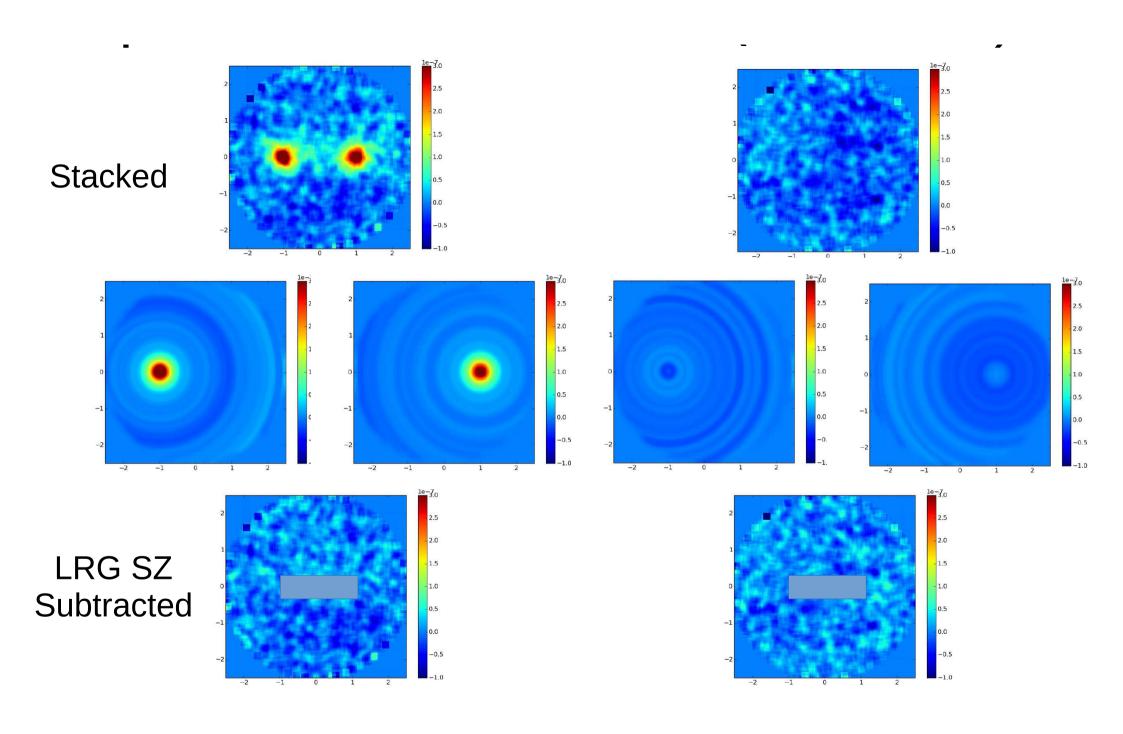
Stacking LRG/SDSS pairs (Ms>11.3, 0.15<z<0.43 (N=28247)) on Planck y-map

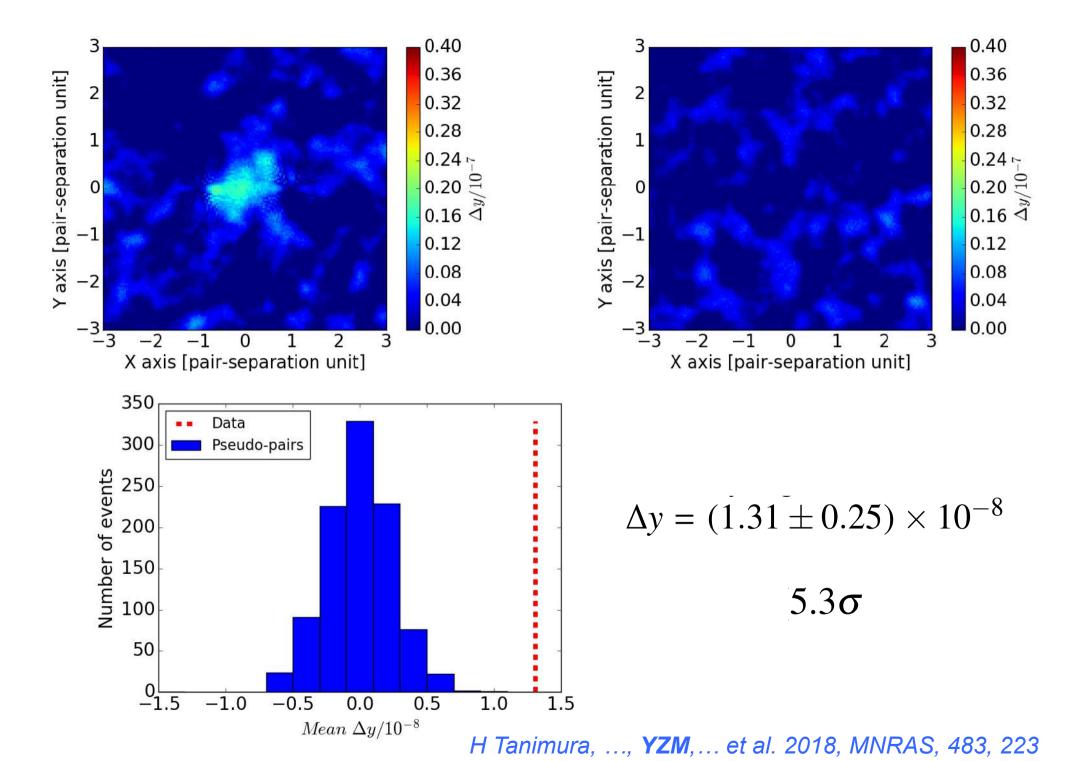
tangential distance: 6-10 $h^{-1}{\rm Mpc}$

radial distance: $\pm 6 h^{-1} \mathrm{Mpc}$









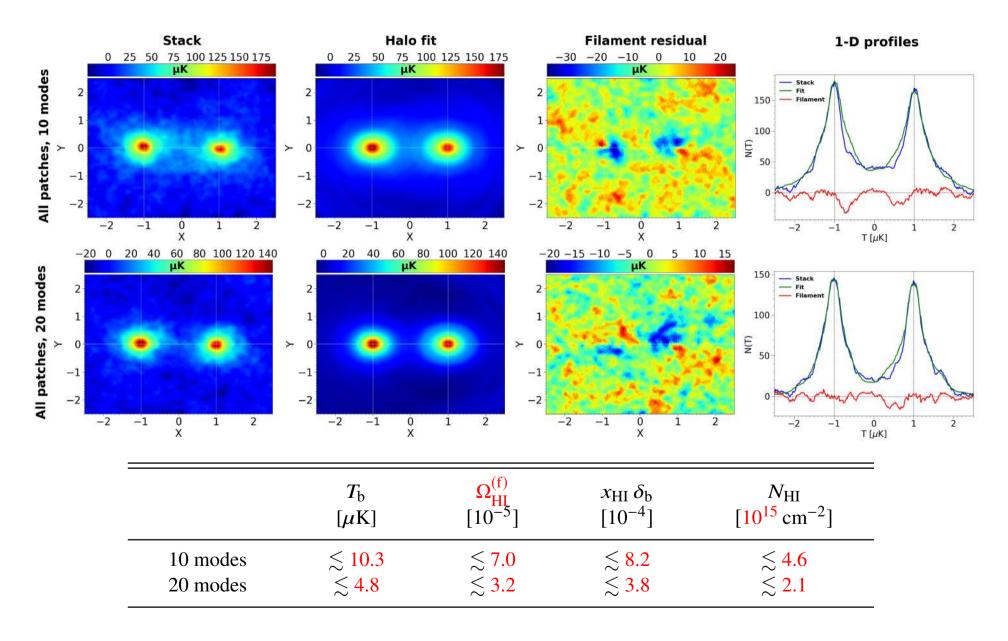
$$y = \int n_{\rm e} \sigma_{\rm T} \frac{k_{\rm B} T_{\rm e}}{m_{\rm e} c^2} \mathrm{d}l$$

$$n_{\rm e} = \overline{n}_{\rm e,i}(1+\delta)$$

$$\overline{n}_{\mathrm{e,i}} = \frac{\chi \rho_{\mathrm{b}}(z)}{\mu_{\mathrm{e}} m_{\mathrm{p}}}$$
 $\chi = \frac{1 - Y_{\mathrm{p}}(1 - N_{\mathrm{H_e}}/2)}{1 - Y_{\mathrm{p}}/2}$

$$\delta_c \left(\frac{T_e}{10^7 \text{ K}} \right) \left(\frac{r_c}{0.5h^{-1} \text{ Mpc}} \right) = 2.7 \pm 0.5$$

Same technique, but applied to **21-cm intensity mapping** (Parkes data)



D. Tramonte, YZM, Y.C. Li, L. Staveley-Smith, 2019, MNRAS



Weak Lensing

YZM. L. Van Waerbeke et al., 2015, JCAP, 09, 046 A. Hojjati, I. McCarthy, J. Harnois-Deraps, YZM et al., 2015, JCAP, 10, 047 A. Hojjati, , YZM,... 2017, JCAP, 471, 1565



Thermal SZ maps X Luminous red galaxies

H Tanimura, ..., **YZM**,... et al. 2018, MNRAS, 483, 223

—>HI (21-cm) intensity mapping X Central galaxies

D. Tramonte, YZM, Y.C. Li, L. Staveley-Smith, 2019, MNRAS

kinetic Sunyaev-Zeldovich effect



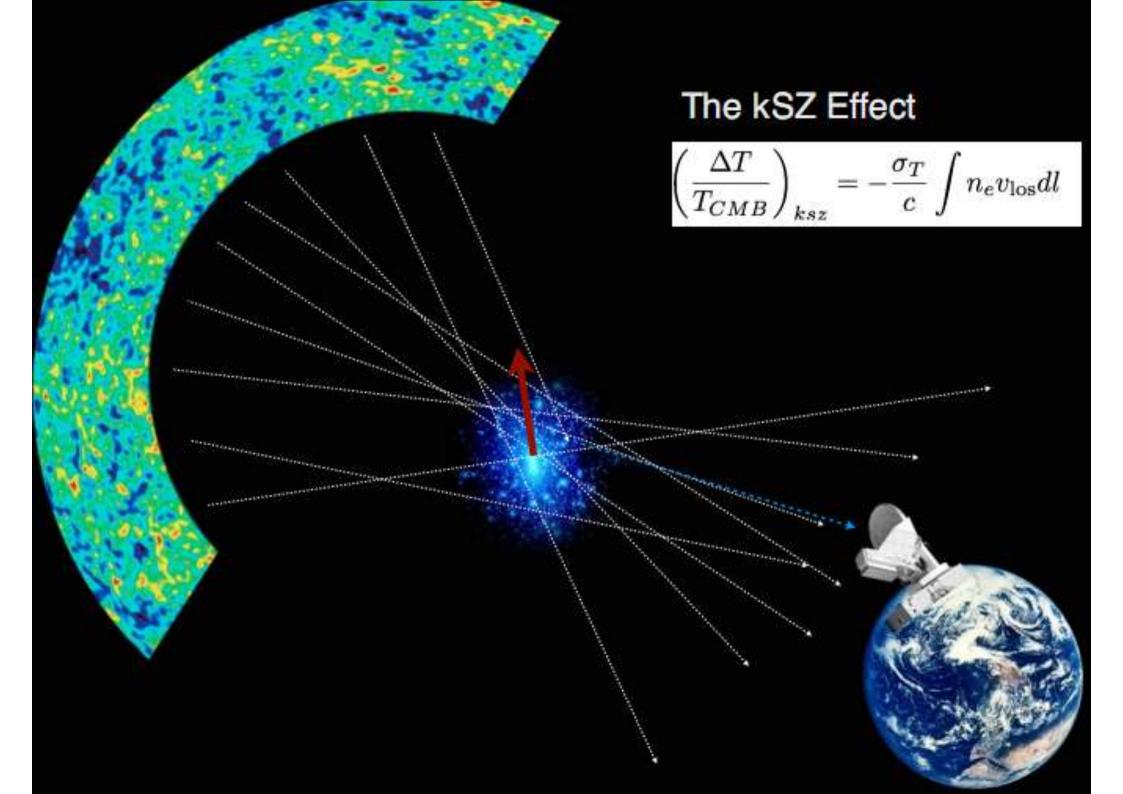
Peculiar velocity field

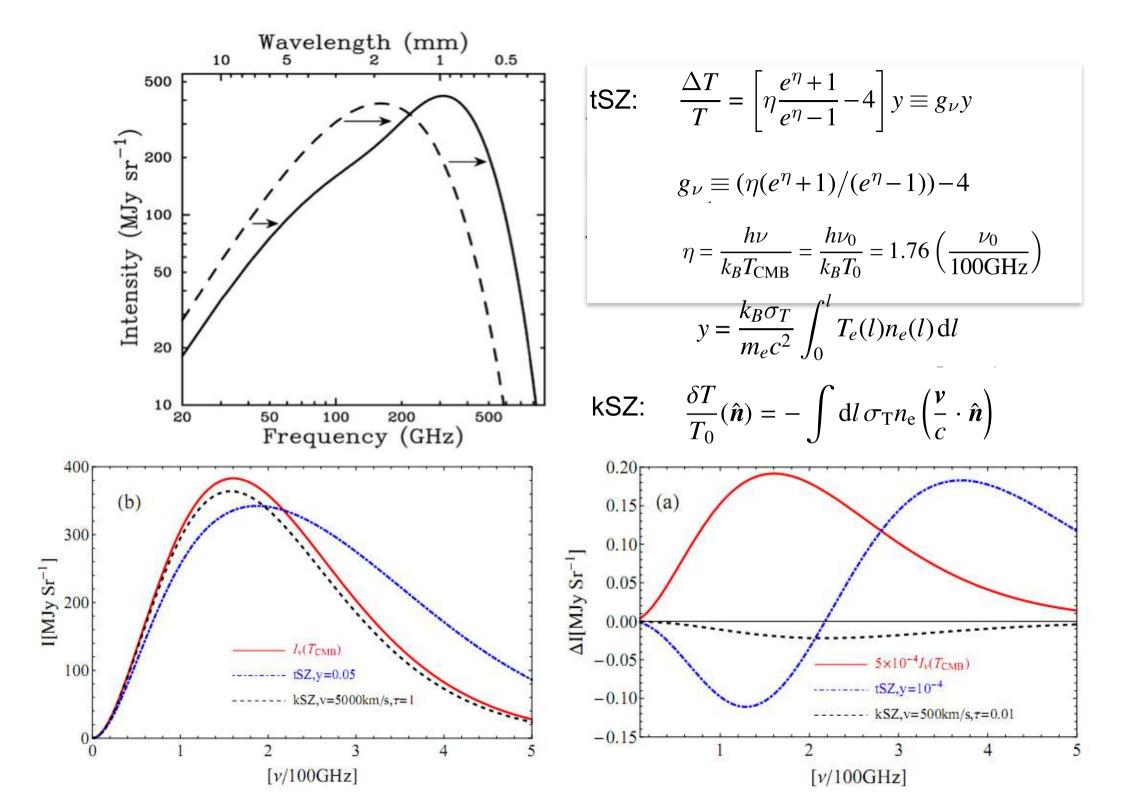
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kinetic SZ effect

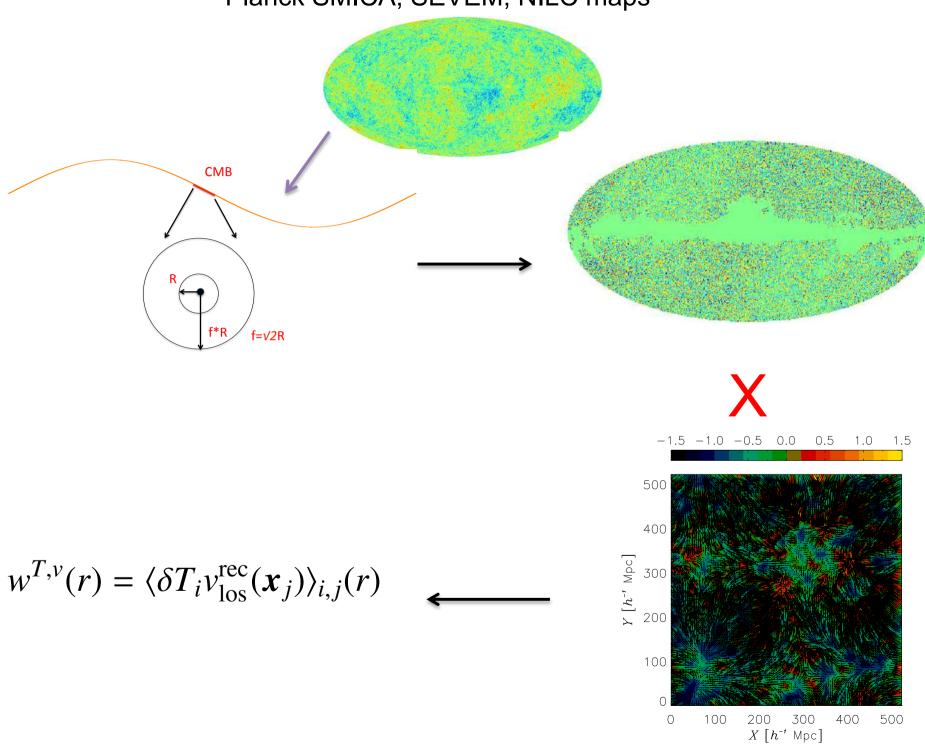


X MCXC clusters

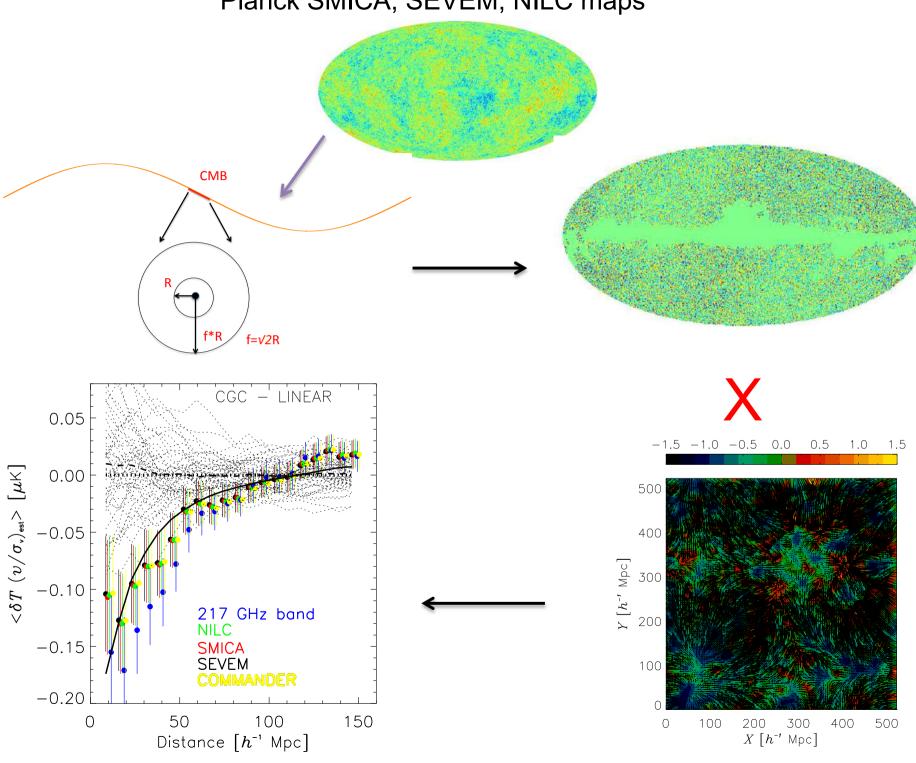


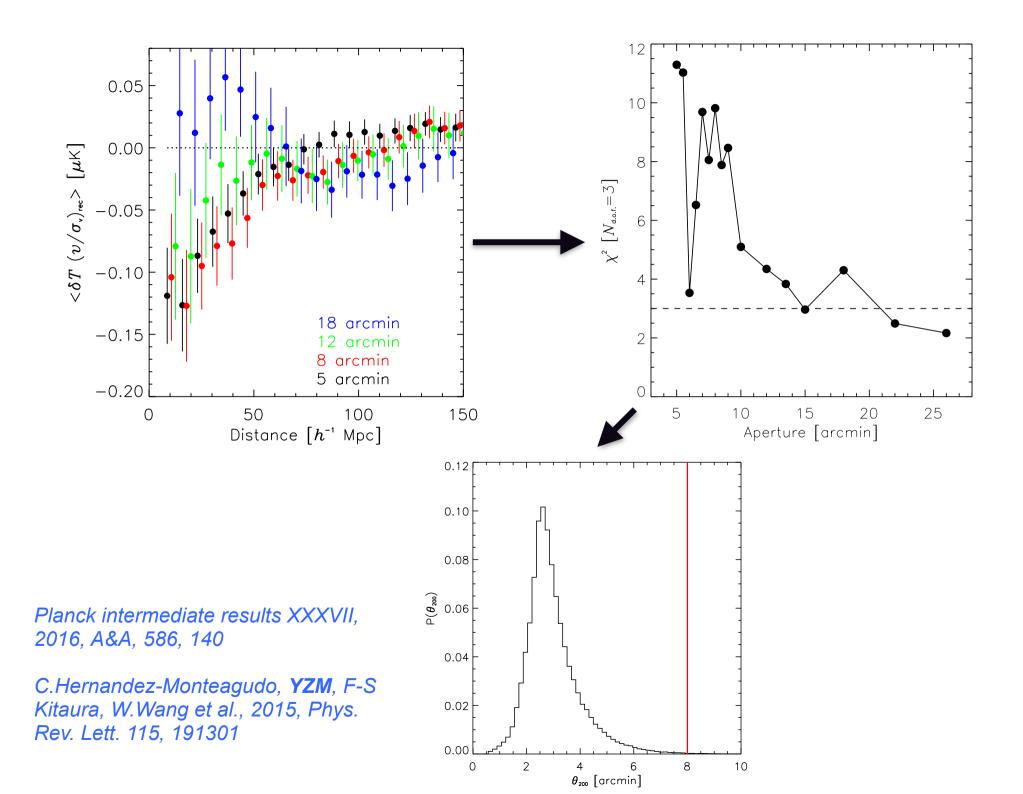


Planck SMICA, SEVEM, NILC maps



Planck SMICA, SEVEM, NILC maps

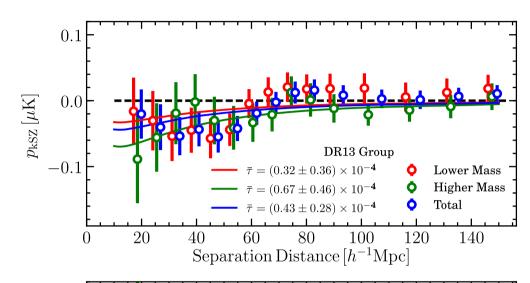




Pairwise kSZ signal

$$\hat{p}_{\text{kSZ}}(r) = -\frac{\sum_{i < j} (\delta T_{\text{kSZ},i} - \delta T_{\text{kSZ},j}) c_{ij}}{\sum_{i < j} c_{ij}^2}$$

$$c_{ij} = \frac{(r_i - r_j)(1 + \cos \theta)}{2\sqrt{r_i^2 + r_j^2 - 2r_i r_j \cos \theta}}$$



$$\bar{\tau} = (0.53 \pm 0.32) \times 10^{-4} (1.65\sigma)$$

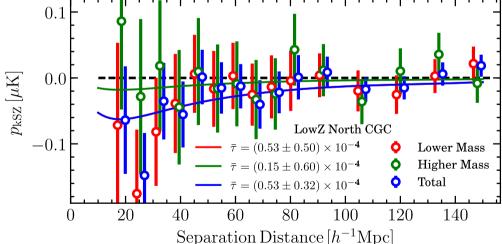
$$\bar{\tau} = (0.30 \pm 0.57) \times 10^{-4} (0.53\sigma)$$

$$\bar{\tau} = (0.43 \pm 0.28) \times 10^{-4} (1.53\sigma)$$

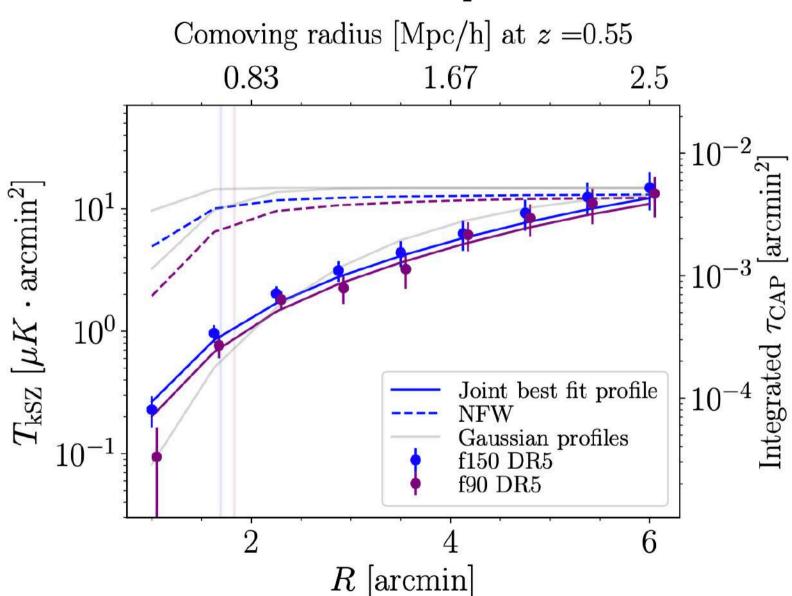
LowZ North CGC;

LowZ South CGC;

DR13 Group.



CMASS kSZ profile



Atacama Cosmology Telescope 2020 results

thermal Sunyaev-Zeldovich effect



X Weak Lensing

YZM. L. Van Waerbeke et al., 2015, JCAP, 09, 046 A. Hojjati, I. McCarthy, J. Harnois-Deraps, YZM et al., 2015, JCAP, 10, 047 A. Hojjati, , YZM,... 2017, JCAP, 471, 1565



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kinetic SZ effect



MCXC clusters

Planck intermediate results LIII, 2018, A&A, 617, A48

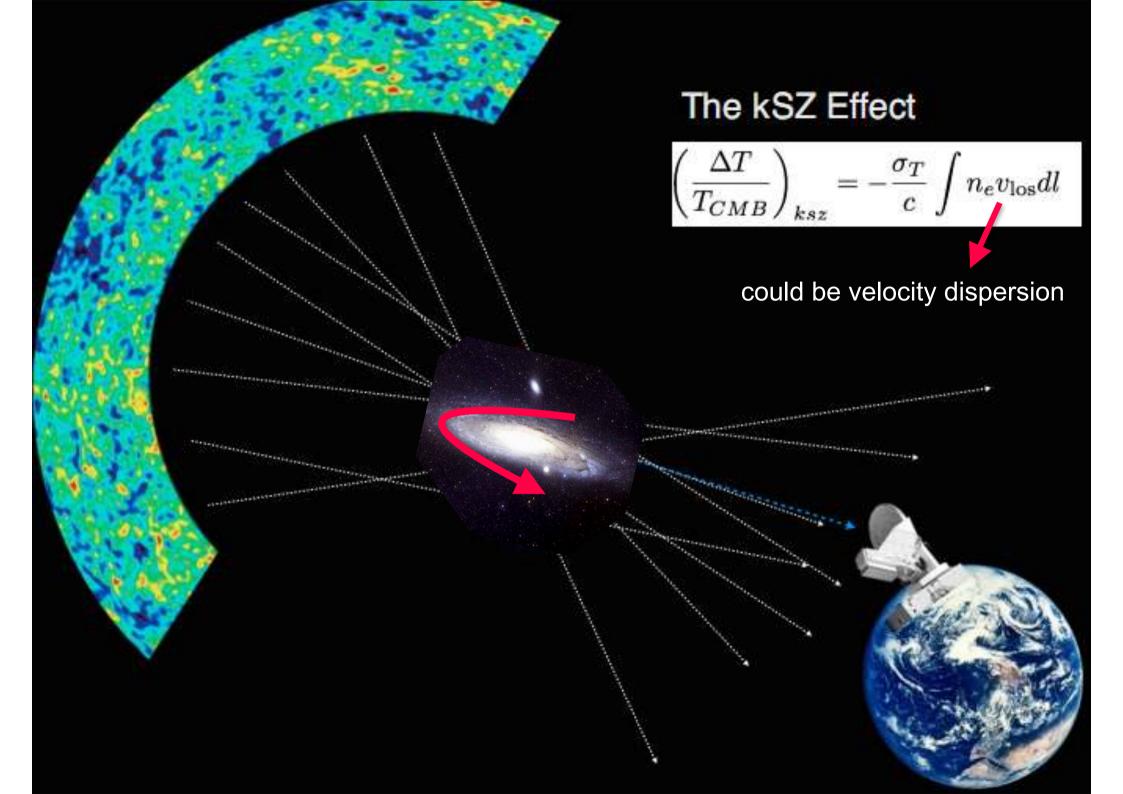
Method	Reference	kSZ data	Tracer type	Tracer data	Significance
Pairwise temperature difference	Hand et al. (2012) ^a Planck Collaboration Int. XXXVII (2016) Hernández-Monteagudo et al. (2015) Soergel et al. (2016) De Bernardis et al. (2017) Sugiyama et al. (2017) ^b Li et al. (2018) ^b	ACT Planck WMAP SPT ACT Planck Planck	Galaxies (spec- z) Galaxies (spec- z) Galaxies (spec- z) Clusters (photo- z) Galaxies (spec- z) Galaxies (spec- z) Galaxies (spec- z)	BOSS III/DR9 SDSS/DR7 SDSS/DR7 1-yr DES BOSS/DR11 BOSS/DR12 BOSS/DR12	2.9σ $1.8-2.5 \sigma$ 3.3σ 4.2σ $3.6-4.1 \sigma$ 2.45σ 1.65σ
$kSZ \times v_{pec}$	Planck Collaboration Int. XXXVII (2016) ^c Schaan et al. (2016) ^c	$\frac{Planck}{ACT}$	Galaxy velocities Galaxy velocities	SDSS/DR7 BOSS/DR10	$3.0 – 3.7 \sigma$ 2.9σ , 3.3σ
$kSZ^2 \times projected$ density field	Hill et al. (2016),	$Planck, \ WMAP$	Projected overdensities	WISE catalogue	3.8 – 4.5σ
kSZ dispersion	Planck Collaboration Int. LIII (2018)	Planck	Clusters	MCXC	2.8σ

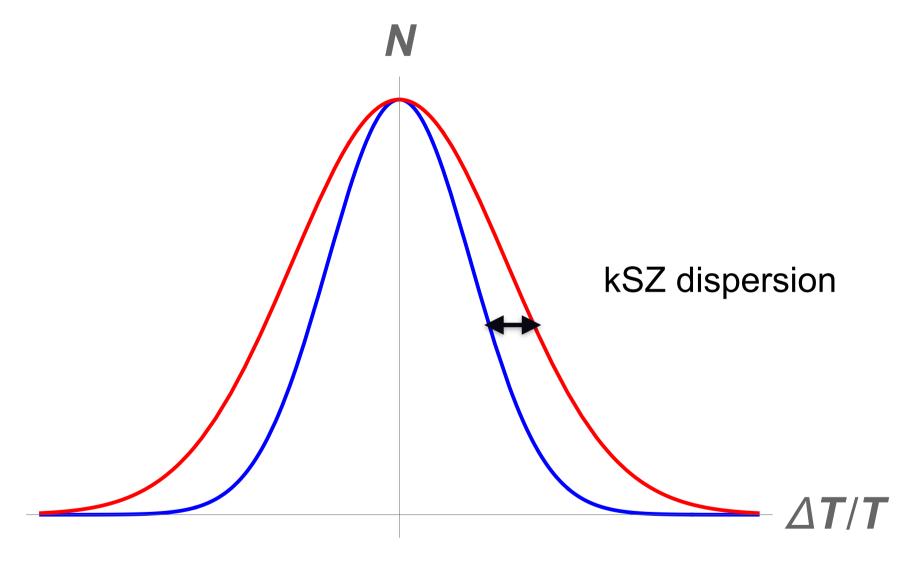
Planck intermediate results

LIII. Detection of velocity dispersion from the kinetic Sunyaev-Zeldovich effect

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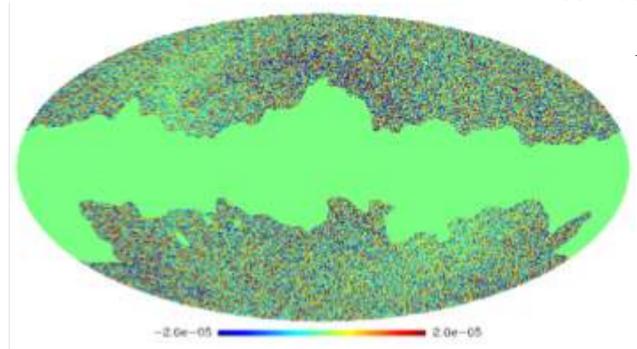
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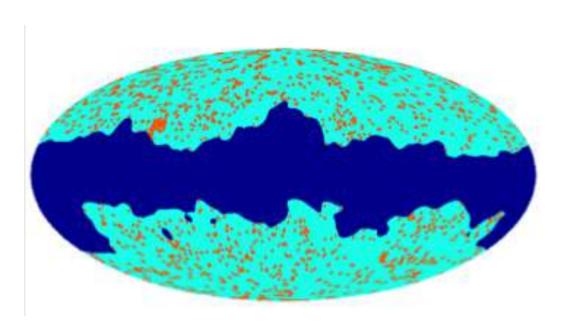
As an analogical example, the average cancer rate above age 60 is N_1 , and for some particular region, some extra condition (unhealthy diet or lifestyle/smoke/stress/poor living condition etc) can boost it up to N_2 ($N_2 > N_1$), the excess rate $N_2 - N_1$ is due to the "extra condition".

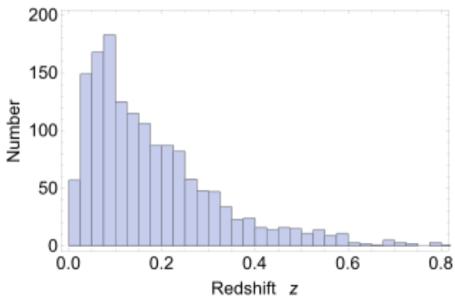
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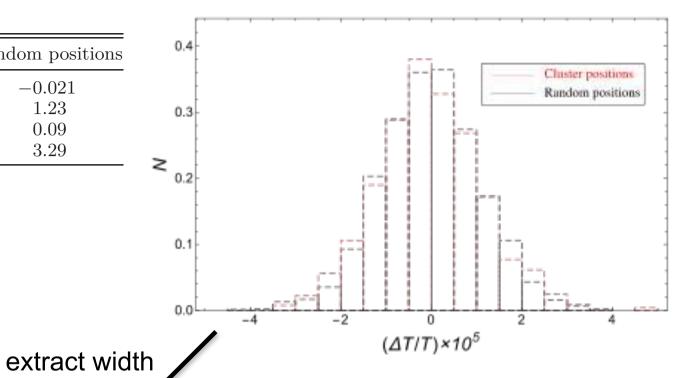
$$W_{\ell} = \frac{B_{\ell}}{B_{\ell}^2 C_{\ell}^{\text{CMB}} + N_{\ell}} = \frac{B_{\ell}}{C_{\ell}^{\text{noise}}}$$

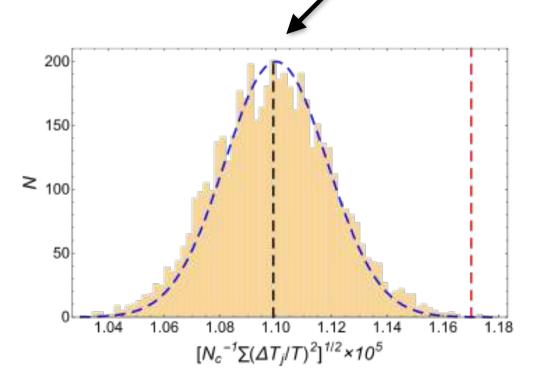
1526 MCXC clusters outside Galactic mask





	True positions	Random positions
Mean	-0.015 1.38 0.37 4.44	-0.021 1.23 0.09 3.29





$$\hat{s^2} = \frac{1}{N_c} \sum_{i} \delta_i^2 - \frac{1}{N_c} \sum_{i} \hat{n}_i^2$$

Map	$E[s^2] \times 10^{11}$	$(V[s^2])^{1/2} \times 10^{11}$	S/N	400	
2D-ILC	1.64	0.48	3.4	300	
SMICA	3.53	0.37	9.4	z	
NILC	2.75	0.38	7.3	200	
SEVEM	3.19	0.40	8.1		
Commander	1.47	0.42	3.5	100	
			,		
$D(a^2 < 0)$	= 0.07%	,		n	
$\Gamma(S_{xy} \leq 0)$	- 0.07/()		U	00 05 10 15 20 25 30

Corrected for lensing contribution:

$$(\hat{s}^2) = (1.35 \pm 0.48) \times 10^{-11}$$

 2.8σ

 $s^2 \times 10^{11}$

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$$\langle v^2 \rangle = (123\,000 \pm 71\,000) \,(\,\mathrm{km}\,\mathrm{s}^{-1})^2$$
$$= \left\langle \left(v_{\mathrm{bulk}} + v_{\mathrm{dis}}\right)^2 \right\rangle = \left\langle v_{\mathrm{bulk}}^2 \right\rangle + \sigma_{\mathrm{dis}}^2$$

Statistical homogeneity on 600 Mpc scale

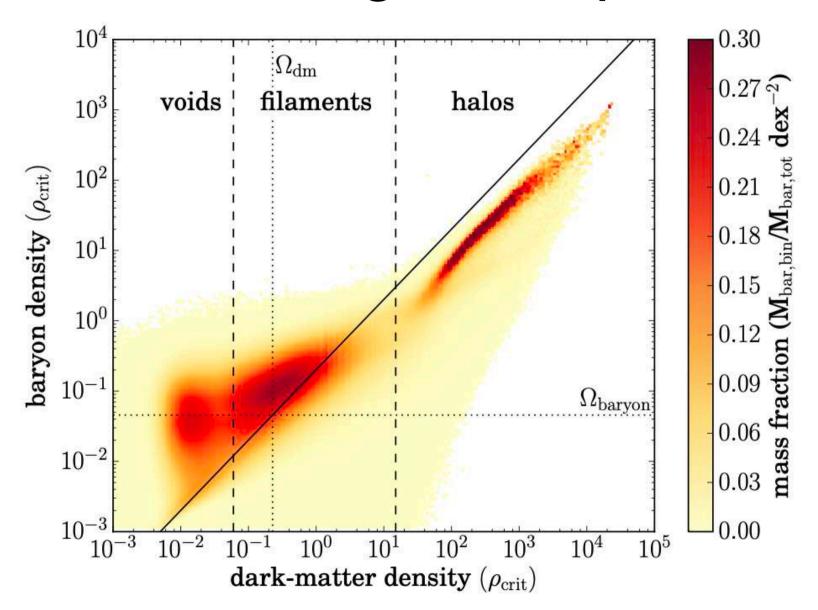
Summary

• Most of the baryons are diffuse and warm-hot IGM with $T = 10^4 - 10^7 \, \mathrm{K}$.

SZ data	LSS tracers	Results
thermal SZ	weak lensing	Gas extends out to $5r_{\rm vir}$, with temperature for $M=10^{12}-10^{16}{\rm M}_{\odot}$ consistent with simulation
thermal SZ	luminous red galaxies	Gas associated with filament is detected at $y = (1.31 \pm 0.25) \times 10^{-8}$ —> $T_{\rm filament} \le 10^7 {\rm K}$
kinetic SZ	,	Maximum detection is reached at $\theta_{\rm AP}=8~{\rm arcmin}$ which is $\sim 3r_{\rm vir}$
kinetic SZ	X-ray selected clusters	$\langle (\Delta T/T)^2 \rangle = (1.35 \pm 0.48) \times 10^{-11}$
		The Universe is homogenous at 600 Mpc.

• Our results suggest that missing baryon at low redshifts is *not* missing, but correlated with underlying LSS density field.

Back to the general picture



	dark matter density	% of total	% of total	% of total	% of total
component	region $(ho_{ m crit})$	dark matter mass	baryonic mass	mass	volume
haloes	> 15	49.2 %	23.2 %	44.9 %	0.16 %
filaments	0.06 - 15	44.5~%	46.4~%	44.8~%	21.6~%
voids	0 - 0.06	6.4~%	30.4~%	10.4~%	78.2~%
ejected material inside voids	0 - 0.06	2.6~%	23.6 %	6.1 %	30.4~%

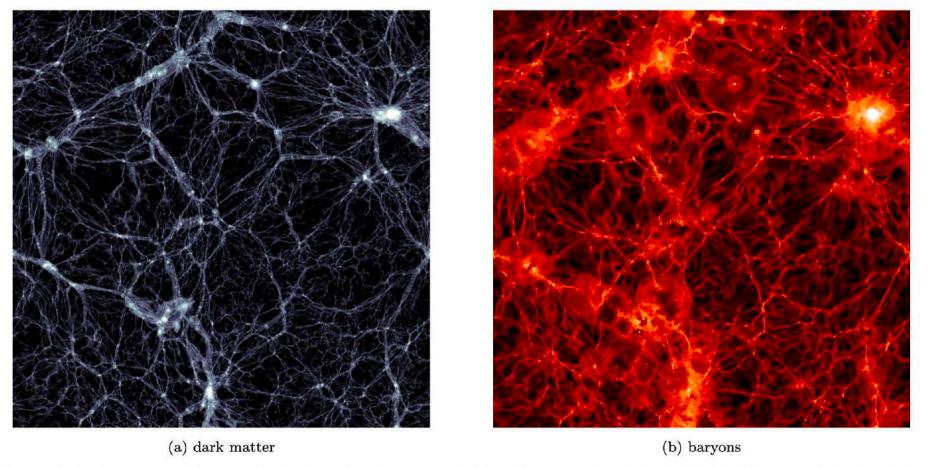
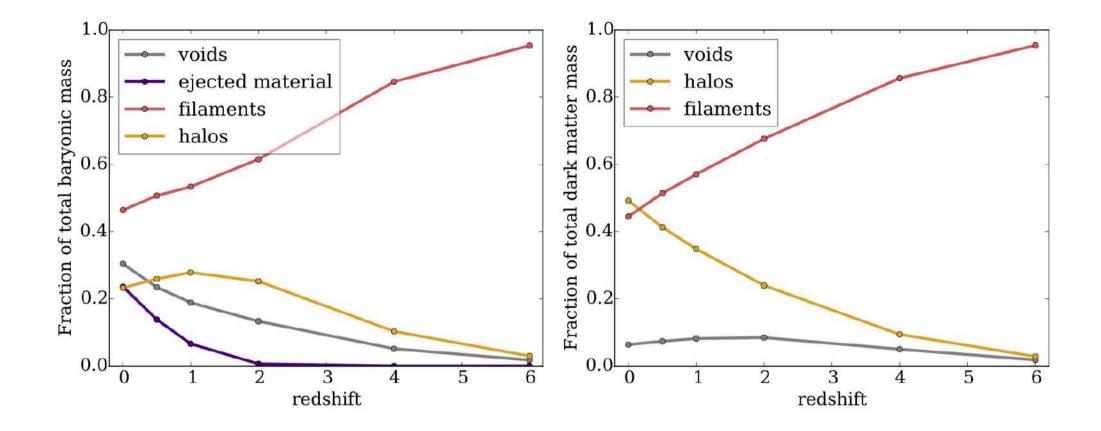


Figure 3. Dark matter and baryon density in a thin slice at z = 0. The slice covers the whole $(106.5 \text{ Mpc})^2$ extent of the simulation and has a thickness of 104 kpc (1 cell).



We should find higher baryon fractions in filaments and voids, but the latter is extremely difficult to measure. But with LSST + CMB-S4 experiments, the sky coverage will be as large as $6000~\rm deg^2$, and very low CMB thermal noise and better angular resolution (~1 arcmin), which has a strong potential to disentangle the signal from filaments and voids.